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Review of Cost-Constrained Minimum Runs Algorithm for Response Sensitivity Analysis of the FRACT3DVS Code

Marsh Hardy

APPLIED RESEARCH ASSOCIATES, INC. 4300 San Mateo Boulevard, NE, Suite A220 Albuquerque, New Mexico 87110

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Environics Directorate Environmental Risk Management Division 139 Barnes Drive, Suite 2 Tyndall Air Force Base FL 32403-5323

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DENNIS O'SULLIVAN, Lt, USAF, BSC

Project Officer

ALLAN M. WEINER, Lt Col, USAF

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Chief, Environmental Risk Management Division

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PREFACE

The work described in this report covers the contract period of July 1995 through April 1996. This work was performed by Applied Research Associates (ARA), Inc., under Contract F08635-93-C-0020, Subtask 8.03, U.S. Air Force AL/EWQ, Barnes Drive, Suite 2, Tyndall Air Force Base, Florida. During the course of this study, there were two project officers, Major Mark H. Smith and Captain Jeff Stinson, BSC. This work was performed under the technical guidance of Mr. Robert E. Walker, ARA. This report was written by Marsh Hardy of ARA and edited by Mr. Walker.

EXECUTIVE SUMMARY

Funnel-and-gate systems are used for in situ groundwater remediation. To design such systems in a cost-effective manner, it is necessary to perform extensive calculations to determine the optimum system dimensions. For performing a good first-order design, a statistically sound model was developed.

Using the multistage design of experiments to perform a limited number of FRACT3DVS computations and stepwise regression, simplified equations are developed to predict the behavior of a funnel and gate system. The four factors included in these equation were identified to be highly significant in predicting behavior of the funnel and gate system. The equations will be useful for evaluating different funnel and gate designs and to make quick predictions in the field (a full FRACT3DVS calculation can take 1-2 days.)

The following conclusions assume the accuracy of the FRACT3DVS code and the comprehensiveness of the four parameters and two response measures studied. (1) Collectively, the first three FRACT3DVS parameters, Kaquifer/Kgate, wf/df, 2*wf/wg, are particularly important in predicting the funnel and gate's operation, especially because of the product of wf/df and 2*wf/wg. (2) It is possible to predict the operation of the funnel and gate system for ground pollution treatment with a high degree of accuracy, using a small, fast-running code on a PC.

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SECTION I

INTRODUCTION

OBJECTIVE

The objective of this effort is to assess the relative contributions of nine variables that affect the FRACT3DVS simulations of a funnel-and-gate system and model those effects in a second, fast-running code.

BACKGROUND

FRACT3DVS is a large computer program used to simulate groundwater flow. A funnel-and-gate system has been devised to treat soil pollutants in situ, that is, in the field.

FRACT3DVS can estimate the amount of pollution captured and flow rates in a funnel and gate system. However, the code is too computer intensive (each run can take 1-2 days on a work station) to be used for the parameter studies needed to design an optimal funnel and gate system. Hence, a simpler, faster running code is required.

SCOPE

The basic scope is to perform FRACT3DVS simulations with different values of the input variables. Using these results we can fit a simple function (i. e., a response surface) that attempts to match the FRACT3DVS output for each set of inputs. Each run of FRACT3DVS takes 1-2 days on a minicomputer or work station and has to be performed off-site by an expert in the use of the code. To get the most information in the least number of runs, it was decided to use a multistage design of experiments. This multistage approach allows us to reduce the number of variables and, therefore, reduce the required number of FRACT3DVS runs. The multistage approach involves a set of "screening runs," followed by additional runs to better define the response sensitivities. "Analysis of variance" (1-3,12) (ANOVA), a statistical method to measure the relative importance of terms in linear models, was used first to find significant linear effects in the screening runs, then later to find overall models of the funnel-and-gate system response measures. Two of the code's output measures were chosen to produce response surface models of the code: relative area and relative flow, in that order of importance.

SECTION II

STAGE 1 -- SCREENING

A complete, quadratic response model in nine variables has 55 terms and would need at least that many runs in order to estimate all of the parameters. Since any significant high order terms are more likely to involve variables that have significant linear effects than those that do not, it is useful to try to reduce the number of variables via screening runs and an ANOVA of the data generated by the screening runs.

A Plackett-Burman (4,5,10,12) experimental design was used for the screening stage of initial runs of the code. Plackett-Burman designs are 2-level designs, run at typical high and low values for each variable. For k variables, Plackett-Burman designs require 4*(int(k/4)+1) runs, i.e., the least multiple of 4, greater than k, which in this case meant 12 runs. The subsequent ANOVA needs at least an additional run, with all variables held at their nominal or central values, to create some model error to use for comparison purposes in the significance tests of the linear response terms. Hence, 13 runs of FRACT3DVS are necessary for the nine factors considered for that screening analysis.

The screening design above was computed for the purpose of identifying important linear effects of the nine FRACT3DVS parameters in the code's simulation of a funnel and gate system. An advantage of the Plackett-Burman design used for the initial screening phase of this design is that it requires fewer than the usual 2*k+1 runs needed for a "one at a time plus center point" design, which would have been 19 runs for this case.

Accordingly, the first experimental design resulted in the X matrix shown in Table 1. The X matrix defines the series of runs given by the Plackett-Burman design with center point, for an initial screening of the nine FRACT3DVS parameters. The results of that screening are used later to compute the next series of runs to perform. Note, the matrix is coded so that - 1=minimal, 0=medial, and 1=maximal values.

TABLE 1. FIRST SCREENING DESIGN.

| Run | Kh | Hydraulic Gradient | Funnel Width | Funnel Depth | Funnel Thickness | Funnel Kh | Gate Height | Gate Width | Dynamic Reaction |
|-----|----|-----------------------|-----------------|-----------------|---------------------|--------------|----------------|---------------|---------------------|
| | | | | | , | | | | |
| 1 | 1 | -1 | 1 | -1 | -1 | -1 | 1 | 1 | 1 |
| 2 | 1 | 1 | -1 | 1 | -1 | -1 | -1 | 1 | 1 1 |
| 3 | -1 | 1 | 1 | -1 | 1 | -1 | -1 | -1 | 1 |
| 4 | 1 | -1 | 1 | 1 | -1 | 1 | -1 | -1 | -1 |
| 5 | 1 | 1 | -1 | 1 | 1 | -1 | 1 | -1 | -1 |
| 6 | 1 | 1 | 1 - | -1 | 1 | 1 | -1 | 1 | -1 |
| 7 | -1 | 1 | 1 | 1 | -1 | 1 | 1 | -1 | 1 |
| 8 | -1 | -1 | 1 | 1 | 1 | -1 | 1 | 1 | -1 |
| 9 | -1 | -1 | -1 | 1 | 1 | 1 | -1 | 1 | 1 |
| 10 | 1 | -1 | -1 | -1 | 1 | 1 | 1 | -1 | 1 |
| 11 | -1 | 1 | -1 | -1 | -1 | 1 | 1 | 1 | -1 |
| 12 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 |
| 13 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

As it turned out, the matrix X given in Table 1 was not entirely representative of the funnel and gate process to be simulated by the FRACT3DVS code. It was not physically consistent to combine high and low values for all pairs of parameters, which is to say that some pairs were correlated.

After a review of this matrix and of the process to be simulated, the nine original parameters were reduced to four independent parameters. The ratio of Kh to funnel Kh became "Kaquifer/Kgate". The ratio of funnel width to funnel depth became "wf/df." The ratio of 2*funnel width to gate width became "2*wf/wg," and hydraulic gradient was now to be called "del_h/del_l." Funnel thickness was deemed to be minimally important to irrelevant. Gate height was to be the same as funnel depth, and dynamic reaction, a chemical reaction, was not to be considered.

A new Plackett-Burman design matrix X, shown in Table 2, was then computed. Note, the nine runs here happen to be the same as 2*k+1, the number of runs required in a one-at-a-time analysis. Plackett-Burman's advantage of fewer number of runs occurs when there are more than 4 variables. Nevertheless, P-B designs have another advantage over one-at-a-time; variables vary throughout the entire set of runs, each variable simultaneously in the presence of each other's variation, which can produce better models.

After the nine new screening runs had been completed the results were analyzed by ANOVA. Relative Area could be represented with a high degree of accuracy as a simple linear model in the first three of the four new parameters -- so accurate that the model explained 97.66 percent of the variation of Relative Area in the screening stage (and which can be expected to change with new, augmenting data).

TABLE 2. PLACKETT-BURMAN INITIAL SCREENING DESIGN WITH CENTER POINT FOR SENSITIVITY ANALYSIS OF 4 FRACT3DVS PARAMETERS.

| Run | Kaquifer/Kgate | wf/df | 2*wf/wg | del_h/del_l | Note: |
|-----|----------------|-------|---------|-------------|----------|
| | | | | | |
| 1 | 4 | 2.0 | 10 | 0.005 | (Case 1) |
| 2 | 1 | 0.5 | 5 | 0.001 | P-B |
| 3 | 1 | 0.5 | 20 | 0.010 | P-B |
| 4 | 1 | 4.0 | 5 | 0.010 | P-B |
| 5 | . 1 | 4.0 | 20 | 0.001 | P-B |
| 6 | 20 | 0.5 | 5 | 0.010 | P-B |
| 7 | 20 | 0.5 | 20 | 0.001 | P-B |
| 8 | 20 | 4.0 | 5 | 0.001 | P-B |
| 9 | 20 | 4.0 | 20 | 0.010 | P-B |

SECTION III

STAGES 2, 3, AND 4

Augmentation of the screening design was reported in "stages" of new runs of decreasing necessity or priority, as shown in Table 3. Stage 1, the screening design was "D-optimally" augmented into a second, higher resolution design, able to estimate second order terms of the significant variables identified by the ANOVA. The D-optimality criterion (5-8) seeks to maximize |X'X|, the determinant of the design's information matrix. For this operation, the non-significant variables are held at their nominal values.

In general, the second, augmenting stage can be divided into second and third stages that first use a 2-level then a 3-level design with ANOVAs after each before producing the final response surface. Here, the low number of variables allowed calculating all augmenting runs after one ANOVA. Stage 2 allowed estimation of all 2nd order terms of the 3 significant variables evident in Stage 1. Stage 3 allowed estimation of the remaining 2nd order terms involving the 4th, so far non-significant variable, "grad h" (del_h/del_l). Stage 4, corresponds to a term for the product of all 4 parameters and ensures a degree of an error lack-of-fit and avoids the problem of an "over-determined" model.

Normalizing transformations of the data can be employed to improve model fit, or transformations can be used to guarantee appropriate bounds on the response model's estimated values. Here, log transforms kept the output values positive.

The seven augmenting runs (10-16) are shown in the augmented X matrix above. A full, quadratic, response surface model was fit to the 16 FRACT3DVS runs, but the analysis based on that model was unreliable since that model's parameter estimates were not, themselves, reliable. A reduced, quadratic, response surface model was required, and one was found using stepwise regression. Its ANOVA table follows showing the model form and its improved parameter estimates.

The reduced model has higher-order terms in second and third parameters only, wf/df and 2*wf/wg, so only those two needed to be coded for a response surface analysis. (The two coding formulae are shown in Table 4.) An analysis of the surface shows a conditional

maximum at wf/df = .3191066 and 2*wf/wg = 4.2285113, shown in Figure 1. The response surface analysis tells us we can maximize the Relative Area measure of performance by designing the funnel and gate system to have parameters as close to these values as is practical to do so. "Canonical" and "ridge" analyses (3,9-12) were two procedures used to find this singularity point.

TABLE 3. AUGMENTED, D-OPTIMAL, SATURATED, 3-LEVEL DESIGN + ERROR.

| Stage | Run | Kqauifer/Kgate | wf/df | 2*wf/wg | del_h/del_l | Relative Area |
|-------|-----|----------------|-------|---------|-------------|---------------|
| 1 | 1 | 4 | 2.0 | 10 | 0.005 | 0.280 |
| | 2 | 1 | 0.5 | 5 | 0.001 | 0.379 |
| | 3 | 1 | 0.5 | 20 | 0.010 | 0.320 |
| | 4 | 1 | 4.0 | 5 | 0.010 | 0.250 |
| | 5 | 1 | 4.0 | 20 | 0.001 | 0.155 |
| | 6 | 20 | 0.5 | 5 | 0.010 | 0.457 |
| 1 | 7 | 20 | 0.5 | 20 | 0.001 | 0.353 |
| | 8 | 20 | 4.0 | 5 | 0.001 | 0.285 |
| | 9 | 20 | 4.0 | 20 | 0.010 | 0.182 |
| | | | | | | |
| 2 | 10 | 4 | 4.0 | 20 | 0.005 | |
| | 11 | 20 | 4.0 | 10 | 0.005 | |
| | | | | | | |
| 3 | 12 | 1 | 4.0 | 5 | 0.001 | |
| | 13 | 4 | 0.5 | 10 | 0.010 | |
| | 14 | 4 | 0.5 | 20 | 0.001 | |
| | 15 | 20 | 0.5 | 10 | 0.001 | |
| | | | | | | |
| 4 | 16 | 1 | 0.5 | 5 | 0.010 | |

The first and fourth FRACT3DVS parameters, Kaquifer/Kgate and del_h/del_l, have monotonically increasing, positively correlated effects on relative area, so no global maximum exists. The higher they go, the greater relative area will be.

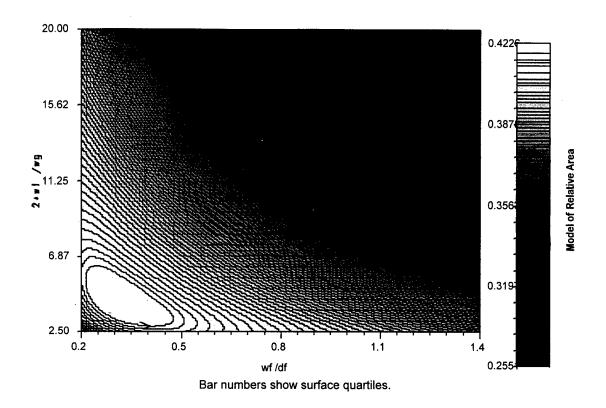


Figure 1. Quadratic Response Surface for Relative Area in Two FRACT3DVS Parameters. (The two other parameters are held at the means of their natural logs.)

The multiple linear regression model for the natural log of relative area and its estimated coefficients are shown in Table 4, the ANOVA table for the model. Table 4 also contains the T-statistics associated with each model parameter. The square of the T statistic is a good measure of the relative importance of each term in the model. This measure is proportional to the variance of the variable in the term and the square of the term's estimated coefficient. The only terms allowed in the model were those that passed the T test at a 0.05 level.

TABLE 4. LINEAR MODEL'S DEPENDENT VARIABLE: LN (RELATIVE AREA).

| Anal | Analysis of Variance (measures and tests for goodness of fit) | | | | | | | | |
|--|---|--|--|--|---------------------|--|--|--|--|
| Source | | DF | Sum of Squares | Mea Squar | | F Value | Prob>F | | |
| Model Error C Total | | 7 8 15 | 1.66818 0.00259 1.67077 | 0.2383 0.0003 | | 736.242 | 0.0001 | | |
| Root MSE Dep Mean C.V. | | 0.01799 -1.25228 -1.43669 | R-square Adj R-sc | | .9985 .9971 | | | | |
| Para | amet | er Estimates (w | ith significance to | ests) | | | | | |
| Variable | DF | Parame Estima | | andard Error | | or HO: eter=0 | Prob > T | | |
| Intercept ln1 cd2 cd3 ln4 cd2cd3 cd2cd2 cd3cd3 | 1 1 1 | -1.155 0.049 -0.288 -0.167 0.015 -0.062 -0.073 -0.031 | 583 0.003 244 0.004 119 0.005 426 0.004 542 0.005 530 0.024 | 121130 379650 170598 527006 448120 539519 414147 271146 | 1 -6 -3 -1 | 7.029 3.060 1.251 1.711 3.442 1.592 3.046 2.457 | 0.0001 0.0001 0.0001 0.0001 0.0088 0.0001 0.0159 0.0395 | | |
| Name | | Definition | | | | | | | |
| ln1 cd2 cd3 ln4 cd2cd3 cd2cd2 cd3cd3 | | | f/df) = (*wf/wg) = (| | | | | | |

Note: A 95% confidence bound for a value of Relative Area predicted by this eq. is (predicted value *or/ 1.0423575), where 1.0423575=exp(t(8,.975)*Root MSE).

SECTION IV

RELATIVE FLOW

Since all analysis and modeling decisions had been based on ANOVAs of relative area, the concern was expressed as to how to transform the results to a response model of relative Qgate (a measure of relative flow). Relative Qgate tended to vary with relative area but not exactly, as shown in Figure 2, which displays a cubic trend with 95 percent bounds for the trend line.

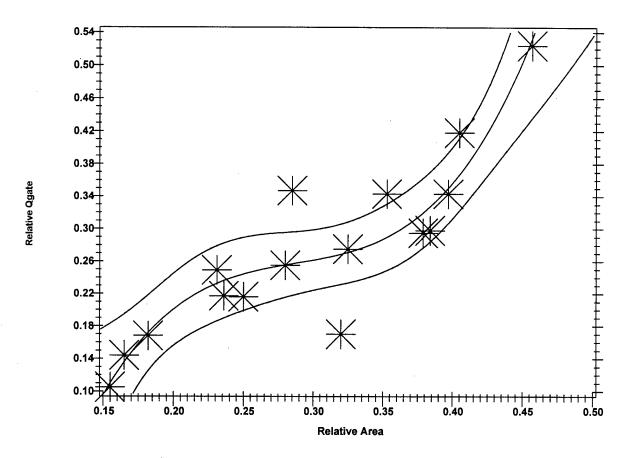


Figure 2. Relative Qgate Trend in Relative Area.

As with relative area, a full, quadratic, response surface model was fit to the 16 FRACT3DVS runs, but an analysis based on that model was unreliable since that model's

parameter estimates were not, themselves, reliable. A reduced, quadratic, response surface model was required, and one was found using stepwise regression. The model for relative Qgate fit the data at least as well as the model for relative area. This was fortuitous, since the decisions as to which variables to concentrate on were based on modeling relative area. The flow model ANOVA, Table 5, follows showing model form and coefficient estimates. As in Table 4, model terms were selected at a 95 percent confidence level.

The reduced model has higher order terms in all 4 FRACT3DVS parameters and linear terms in the 1st and 3rd parameters only, Kaquifer/Kgate and 2*wf/wg. Such a model cannot be formally analyzed for regions of optimality by the SAS response surface procedure available and was not attempted herein. Running this model with a fine 4D mesh is another way to find regions of optimality, and the results can be presented graphically. This could be a topic of some future investigation, but we know relative area and relative flow increase together.

TABLE 5. LINEAR MODEL'S DEPENDENT VARIABLE: LN(RELATIVE QGATE).

| Α | analysis of Variance | (measu | res and tests | for goodness | of fit) | |
|------------------------------|--|--------------------|-----------------------|--------------------------|--------------------------|------------------|
| Source | Sum df Squa | - | Mean Square | F Value | Prob>F | |
| Model | 8 2.58 7 0.00 | | 0.32359 | 1494.499 | 0.0001 | |
| Error C Total | 7 0.00 15 2.59 | | 0.00022 | | | |
| CIOCAL | 13 2.39 | 022 | | | | |
| Root MSE Dep Mean C.V. | | -square dj R-se | | | | |
| | Parameter Estimates | (with | significance | tests) | | |
| Variable | Definition | df | Parameter Estimate | Standard Error | T for H0: Parameter=0 | Prob> T |
| intercept | | 1 | -0.484772 | 0.05102584 | -9.501 | 0.0001 |
| ln1 . | <pre>ln(Kaquifer/Kgate ln(wf/df)</pre> |) 1 | 0.332230 | 0.01618190 | 20.531 | 0.0001 |
| ln3 | ln(2*wf/wg) | 1 | -0.575412 | 0.04126705 | -13.944 | 0.0001 |
| ln4 | <pre>ln(del_h/del_l)</pre> | • | (0.) | | | 0.0045 |
| ln1ln2 | ln1 * În2 | 1 | -0.013979 | 0.00339552 0.00468619 | -4.117 3.316 | 0.0045 0.0128 |
| ln1ln3 | ln1 * ln3 | 1 1 | 0.015540 -0.090229 | 0.00468619 | -36.983 | 0.0128 |
| ln2ln3 ln3ln4 | ln2 * ln3 ln3 * ln4 | 1 | -0.030229 | 0.00697718 | -3.511 | 0.0098 |
| 1n31n4 1n11n1 | ln1 * ln1 | 1 | -0.059383 | 0.00415047 | -14.308 | 0.0001 |
| ln4ln4 | ln4 * ln4 | 1 | -0.003971 | 0.00135214 | -2.937 | 0.0218 |

Note: A 95% confidence bound for a value of Relative Flow predicted by this eq. is (predicted value *or/ 1.0354014), where 1.0354014=exp(t(7,.975)*Root MSE).

SECTION V

SUMMARY AND CONCLUSIONS

Using the multistage design of experiments to perform a limited number of FRACT3DVS computations and stepwise regression, simplified equations are developed to predict the behavior of a funnel and gate system. The four factors included in these equation were identified to be highly significant in predicting behavior of the funnel and gate system. The equations will be useful for evaluating different funnel and gate designs and to make quick predictions in the field (a full FRACT3DVS calculation can take 1-2 days.)

The following conclusions assume the accuracy of the FRACT3DVS code and the comprehensiveness of the four parameters and two response measures studied. (1) Collectively, the first three FRACT3DVS parameters, Kaquifer/Kgate, wf/df, 2*wf/wg, are particularly important in predicting the funnel and gate's operation, especially because of the product of wf/df and 2*wf/wg. (2) It is possible to predict the operation of the funnel and gate system for ground pollution treatment with a high degree of accuracy, using a small, fast-running code on a PC.

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